

To measure the volume of an object, two lengths  $l_1$  and  $l_2$  are measured.

$$l_1 = 10.25 \pm 0.05 \text{ cm} \rightarrow \Delta a$$

$$l_2 = 15.45 \pm 0.05 \text{ cm}$$

Calculate:

- (a) the % uncertainty in  $l_1$
- (b) the % uncertainty in  $l_2$
- (c) the area of the object
- (d) the % uncertainty in the area.

$$\begin{aligned} \% \text{ uncertainty } (l_1) &= \frac{\Delta a}{a} = \frac{0.05 \text{ cm}}{10.25 \text{ cm}} * 100 = \\ &= .4878 \% \\ &= \boxed{.5\%} \text{ (1 SF) } (\infty) \end{aligned}$$

To measure the volume of an object, two lengths  $l_1$  and  $l_2$  are measured.

$$l_1 = 10.25 \pm 0.05 \text{ cm}$$

$$l_2 = 15.45 \pm 0.05 \text{ cm} \Rightarrow \Delta a$$

Calculate:

- (a) the % uncertainty in  $l_1$
- (b) the % uncertainty in  $l_2$
- (c) the area of the object
- (d) the % uncertainty in the area.

$$\% \text{ uncertainty } (l_2) = \frac{\Delta a}{a} * 100 = \frac{0.05 \text{ cm}}{15.45 \text{ cm}} * 100$$

$$= .3236\%$$

$$= \boxed{.3\%} \text{ (1SF)}$$

To measure the volume of an object, two lengths  $l_1$  and  $l_2$  are measured.

$$l_1 = 10.25 \pm 0.05 \text{ cm}$$

$$l_2 = 15.45 \pm 0.05 \text{ cm}$$

Calculate:

- (a) the % uncertainty in  $l_1$
- (b) the % uncertainty in  $l_2$
- (c) the area of the object
- (d) the % uncertainty in the area.

$$158.4 \pm 1.3 \text{ cm}^2$$

$$(A) \text{ Area} = l \times w$$

$$A = l_1 \times l_2$$

$$A = (10.25 \text{ cm})(15.45 \text{ cm})$$

$$A = 158.4 \text{ cm}^2$$

$$A_{\max} = l_{1 \max} \times l_{2 \max}$$

$$A_{\max} = (10.3 \text{ cm})(15.5 \text{ cm}) = 159.65 \text{ cm}^2$$

$$A_{\min} = l_{1 \min} \times l_{2 \min}$$

$$(10.2 \text{ cm})(15.4 \text{ cm}) = 157.08 \text{ cm}^2$$

$$\Delta A = \frac{A_{\max} - A_{\min}}{2} = \frac{159.65 - 157.08}{2} = 1.285 \text{ cm}^2$$
$$= 1.3 \text{ cm}^2$$

To measure the volume of an object, two lengths  $l_1$  and  $l_2$  are measured.

$$l_1 = 10.25 \pm 0.05 \text{ cm}$$

$$l_2 = 15.45 \pm 0.05 \text{ cm}$$

Calculate:

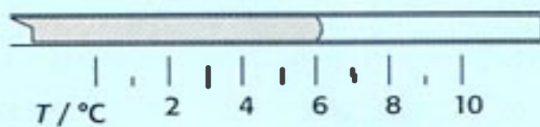
- (a) the % uncertainty in  $l_1$
- (b) the % uncertainty in  $l_2$
- (c) the area of the object
- (d) the % uncertainty in the area.

$$\begin{aligned} \text{\% uncertainty} &= \text{\% uncert}_{l_1} + \text{\% uncert}_{l_2} \\ \text{(product)} &= .5\% + .3\% \\ &= \boxed{.8\%} \end{aligned}$$

$$\boxed{158.4} \pm \boxed{1.3} \text{ cm}^2$$

$$\begin{aligned} \text{\% uncertainty} &= \frac{\Delta A}{A} * 100 = \frac{1.3}{158.4} * 100 = .8207\% \\ &= \boxed{.82\%} \end{aligned}$$

- 1** The diagram below shows the position of the meniscus of the mercury in a mercury-in-glass thermometer.



Which of the following best expresses the indicated temperature with its uncertainty?

- A**  $(6.0 \pm 0.5)^\circ\text{C}$
- B**  $(6.1 \pm 0.1)^\circ\text{C}$
- C**  $(6.2 \pm 0.2)^\circ\text{C}$
- D**  $(6.2 \pm 0.5)^\circ\text{C}$

[1]

- 3** An ammeter has a zero offset error. This fault will affect
- A** neither the precision nor the accuracy of the readings.
  - B** only the precision of the readings.
  - C** only the accuracy of the readings.
  - D** both the precision and the accuracy of the readings.
- [1]

A student measures a distance several times. The readings lie between 49.8 cm and 50.2 cm. This measurement is best recorded as

A  $49.8 \pm 0.2$  cm.

B  $49.8 \pm 0.4$  cm.

C  $50.0 \pm 0.2$  cm.

D  $50.0 \pm 0.4$  cm.

(1)

The power dissipated in a resistor of resistance  $R$  carrying a current  $I$  is equal to  $I^2R$ . The value of  $I$  has an uncertainty of  $\pm 2\%$  and the value of  $R$  has an uncertainty of  $\pm 10\%$ . The value of the uncertainty in the calculated power dissipation is

- A  $\pm 8\%$ .
- B  $\pm 12\%$ .
- C  $\pm 14\%$ .
- D  $\pm 20\%$ .

$$I^2R$$

(1)

$$2\%I + \%R$$
$$2(2\%) + 10\%$$
$$14\%$$



When a force  $F$  of  $(10.0 \pm 0.2)$  N is applied to a mass  $m$  of  $(2.0 \pm 0.1)$  kg, the percentage uncertainty attached to the value of the calculated acceleration  $\frac{F}{m}$  is

- A 2%.
- B 5%.
- C 7%.
- D 10%.

$$\% \text{ uncert.}_F = \frac{0.2}{10.0} \times 100 = 2\%$$

$$\% \text{ uncert.}_m = \frac{0.1}{2.0} \times 100 = 5\%$$

$$\% \text{ uncert.}_a = \% F + \% m = 7\%$$

The length of each side of a sugar cube is measured as 10mm with an uncertainty of  $\pm 2$ mm. Which of the following is the absolute uncertainty in the volume of the sugar cube?

- A.  $\pm 6 \text{ mm}^3$
- B.  $\pm 8 \text{ mm}^3$
- C.  $\pm 400 \text{ mm}^3$
- D.  $\pm 600 \text{ mm}^3$

$10 \text{ mm} \pm 2 \text{ mm}$        $\Delta V \% = 60\%$

$l \pm \Delta l$        $V = 1000 \text{ mm}^3$

$V = l^3 \pm 3 \% \text{ uncert}$

$\% l = \frac{2 \text{ mm}}{10 \text{ mm}} * 100 = 20\%$

$\frac{\Delta a}{a} * 100 = \% \text{ uncert}$

$\Downarrow$   
absolute uncertainty of volume  
 $= 60\% * 1000 \text{ mm}^3$

The current in a resistor is measured as  $2.00\text{A} \pm 0.02\text{A}$ . Which of the following correctly identifies the absolute uncertainty and the percentage uncertainty in the current?

	Absolute uncertainty	Percentage uncertainty
A.	$\pm 0.02\text{A}$	$\pm 1\%$
B.	$\pm 0.01\text{A}$	$\pm 0.5\%$
C.	$\pm 0.02\text{A}$	$\pm 0.01\%$
D.	$\pm 0.01\text{A}$	$\pm 0.005\%$

$$2.00\text{A} \pm 0.02\text{A}$$

$\Delta a \Rightarrow$  absolute uncertainty

$$\% \text{uncert} = \frac{\Delta a}{a} * 100 = \frac{.02}{2.00} * 100 = 1\%$$